

# Cryptography

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# Stream and Block Ciphers

- Both uses symmetric encryption key
- Stream Cipher: It encrypts a digital data stream one bit or 1 byte at a time
- Block Ciphers: In this a block of plain text is treated as a whole and used to produce the ciphertext of equal length, Typically a block size of 64 or 128 bits.



# Block Ciphers



# Block Cipher

- Plaintext and ciphertext consists of fixed sized blocks
- Ciphertext obtained from plaintext by iterating a round function
- Input to round function consists of key and the output of previous round
- Usually implementation friendly. Gives a high throughput





# Feistel Cipher (1973 IBM)

- Feistel cipher refers to splitting the plaintext into two equal parts
- Split plaintext block into left and right halves: Plaintext =  $(L_0, R_0)$
- These two halves of the data pass through  $n$  rounds of processing and then combine to produce the ciphertext block
- For each round  $i=1,2,\dots,n$ , compute
$$L_i = R_{i-1}$$
$$R_i = L_{i-1} \oplus F(R_{i-1}, K_i)$$
where  $F$  is round function and  $K_i$  is subkey (*refer next slide for it*)
- Ciphertext =  $(L_n, R_n)$



# Feistel Cipher: Sub Key

- On the right half we apply a function and in the function, we use a subkey generated from the master key (main key)
- A substitution is performed on the left half of the data. This is done by applying a round function to the right half of the data followed by the XOR of the output of that function and the left half of the data.
- That's count the first round.
- All rounds have the same structure
- All conventional block encryption algorithms including data encryption standard (DES) are based on Feistel Cipher Structure.

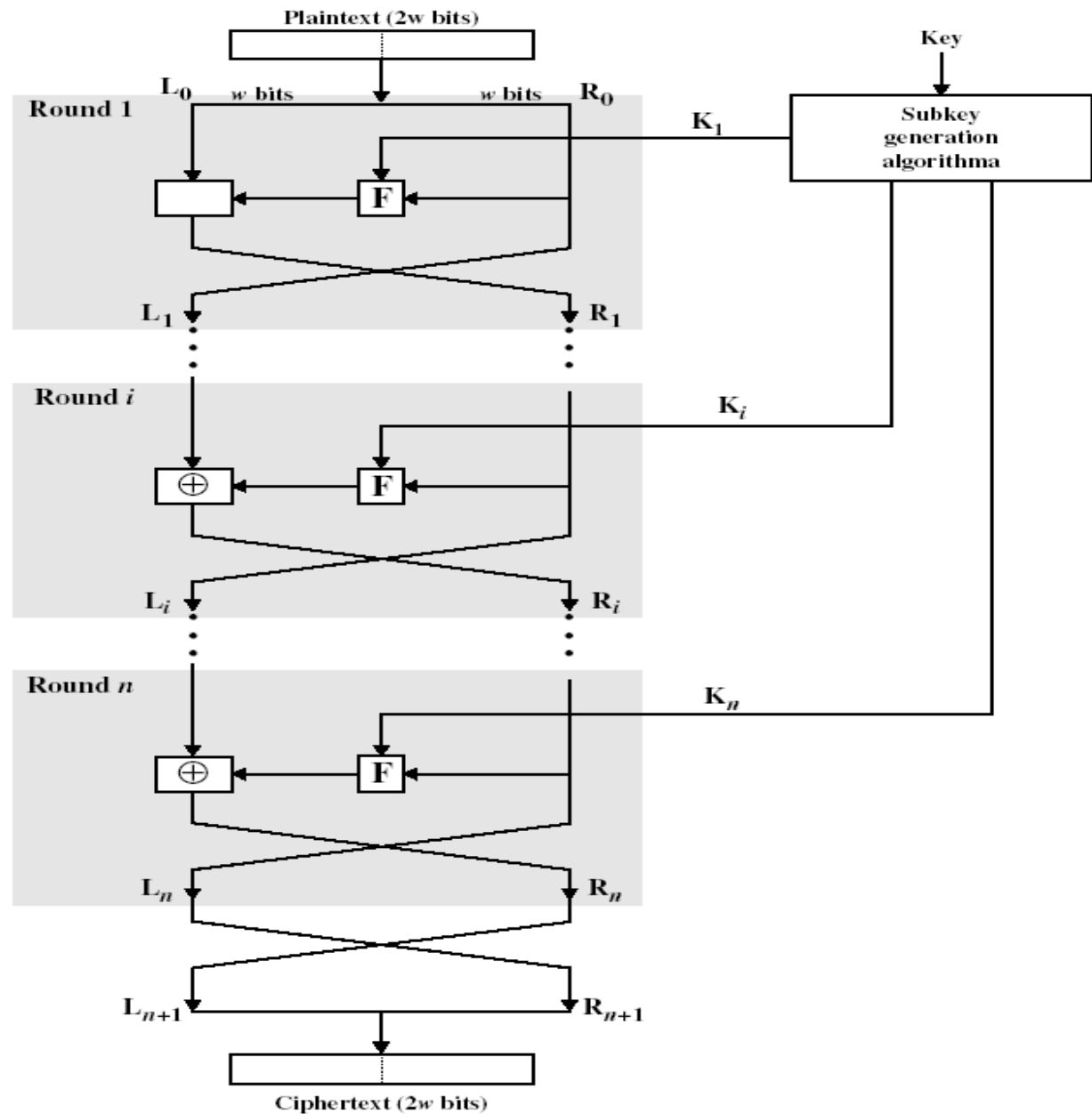


# Feistel Cipher

- Decryption: Ciphertext =  $(L_n, R_n)$
- For each round  $i=n, n-1, \dots, 1$ , compute
$$R_{i-1} = L_i$$
$$L_{i-1} = R_i \oplus F(R_{i-1}, K_i)$$
where  $F$  is round function and  $K_i$  is subkey
- Plaintext =  $(L_0, R_0)$
- Formula “works” for any function  $F$
- But only secure for certain functions  $F$



# Classical Feistel Network



# Design Features of Feistel Network

- **Block Size:** (larger block means greater security).
- **Key Size:** 56-128 bits.
- **Number of Rounds:** a single round offers inadequate security; a typical size is 16 rounds.
- **Sub-key Generation Algorithms:** greater complexity should lead to a greater difficulty of cryptanalysis.
- **Round function:** Again, greater complexity generally means greater resistance to cryptanalysis.



# Block Ciphers in Practice

## Data Encryption Standard (DES)

- Developed by IBM and adopted by NIST in 1977
- 64-bit blocks and 56-bit keys
- Small key space makes exhaustive search attack feasible since late 90s

## Triple DES (3DES)

- Nested application of DES with three different keys  $K_A$ ,  $K_B$ , and  $K_C$
- Effective key length is 168 bits, making exhaustive search attacks unfeasible
- $C = E_{K_C}(D_{K_B}(E_{K_A}(P)))$ ;  $P = D_{K_A}(E_{K_B}(D_{K_C}(C)))$
- Equivalent to DES when  $K_A=K_B=K_C$  (backward compatible)

## Advanced Encryption Standard (AES)

- Selected by NIST in 2001 through open international competition and public discussion
- 128-bit blocks and several possible key lengths: 128, 192 and 256 bits
- Exhaustive search attack not currently possible
- AES-256 is the symmetric encryption algorithm of choice

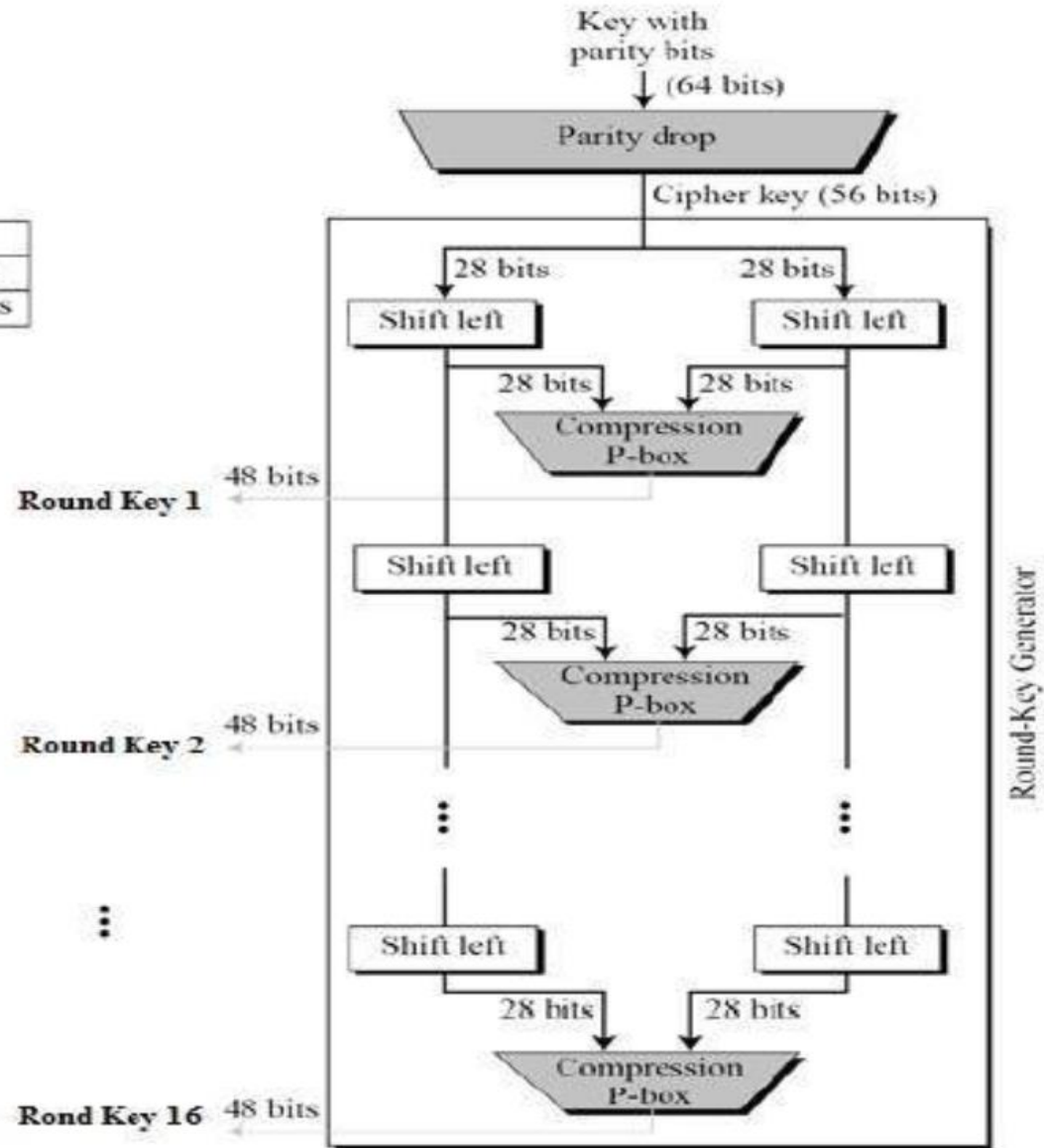


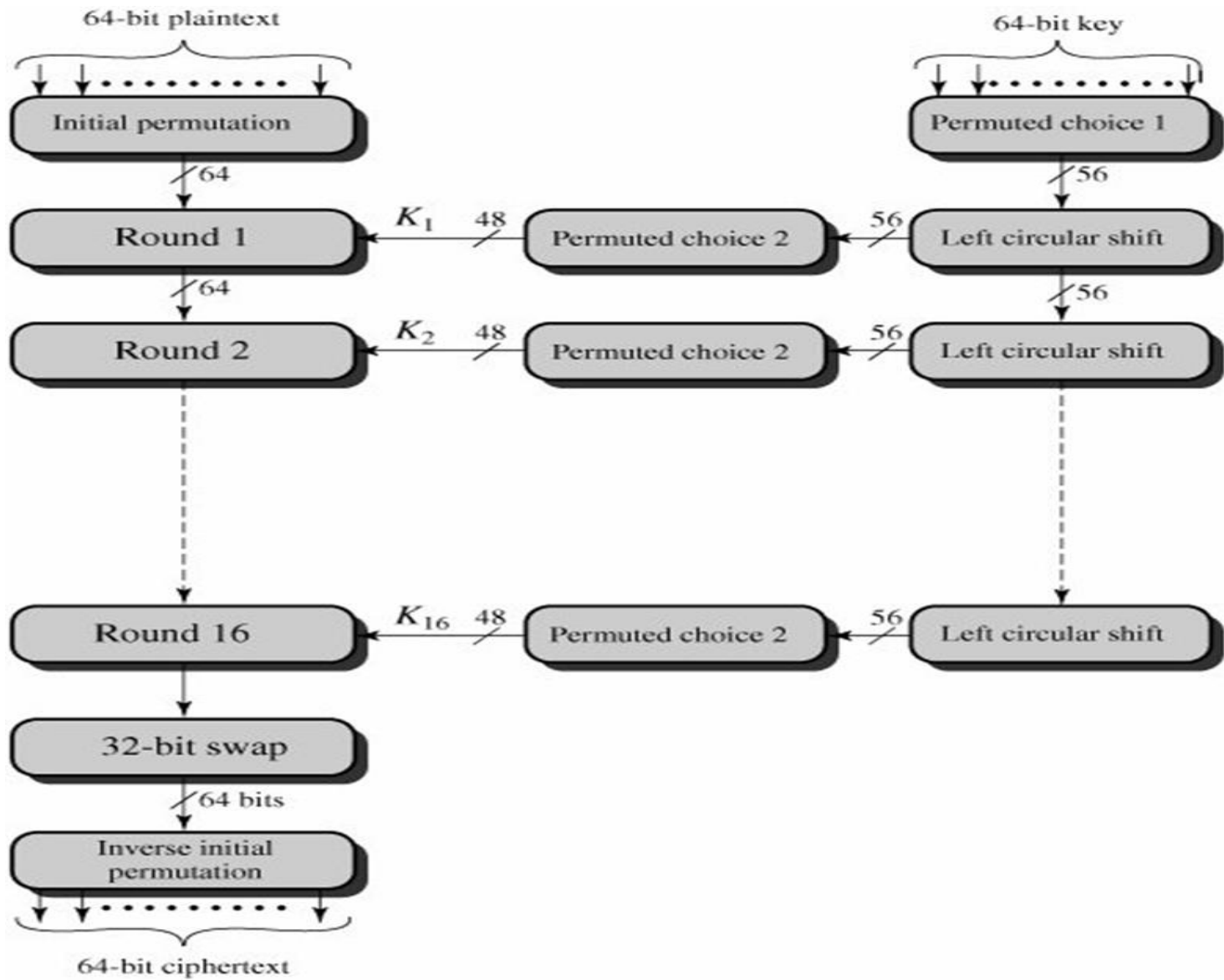
# Data Encryption Standard (DES)

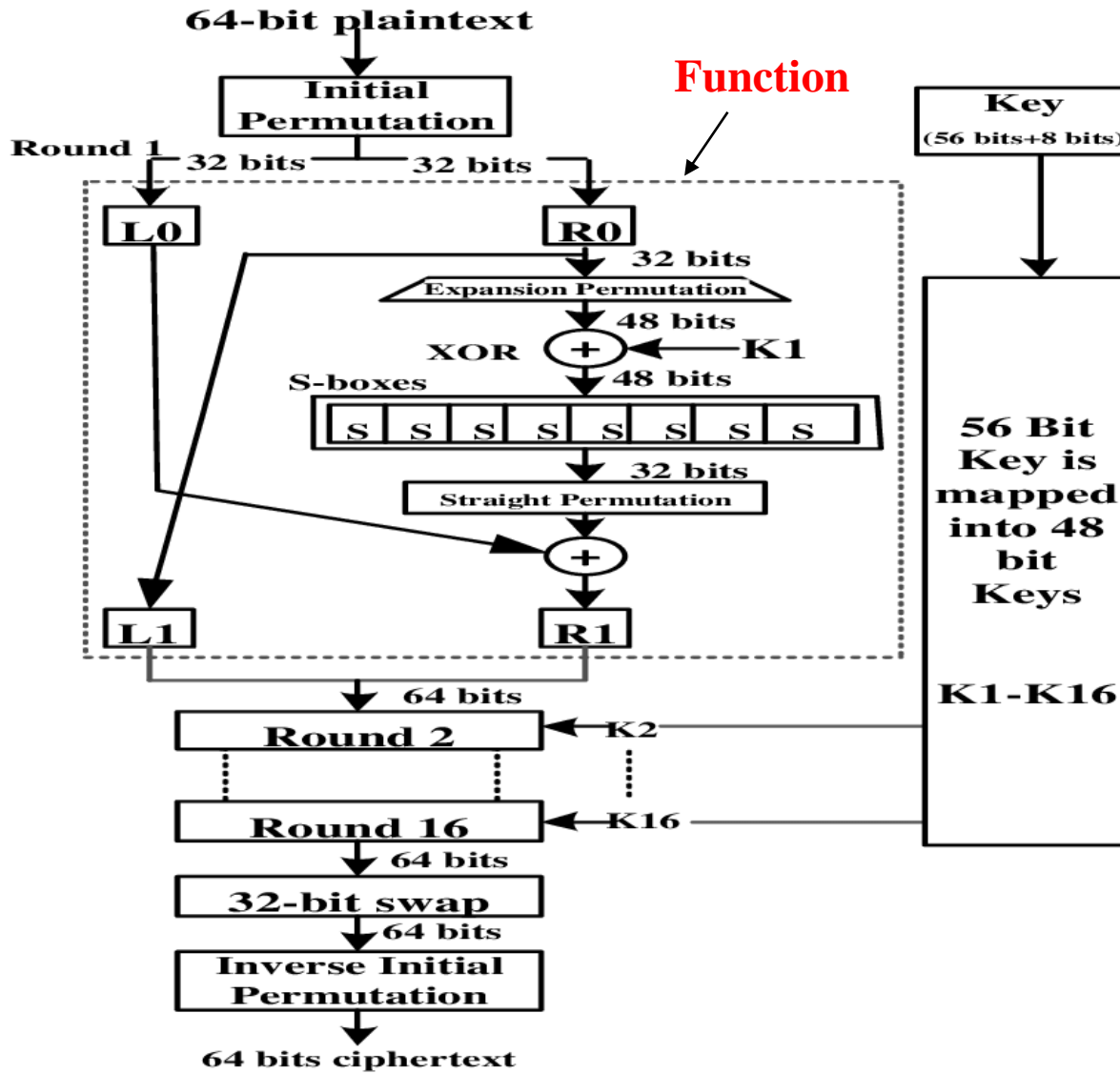
- Block Cipher
- Symmetric cipher (same Keys for the encryption and decryption)
- 64 bit plaintext block
- 16 feistel round
  
- Steps in DES:
  - I. Initial Permutation
  - II. 16 Feistel rounds
  - III. Swapping or left right swap
  - IV. Final permutation or inverse initial permutation



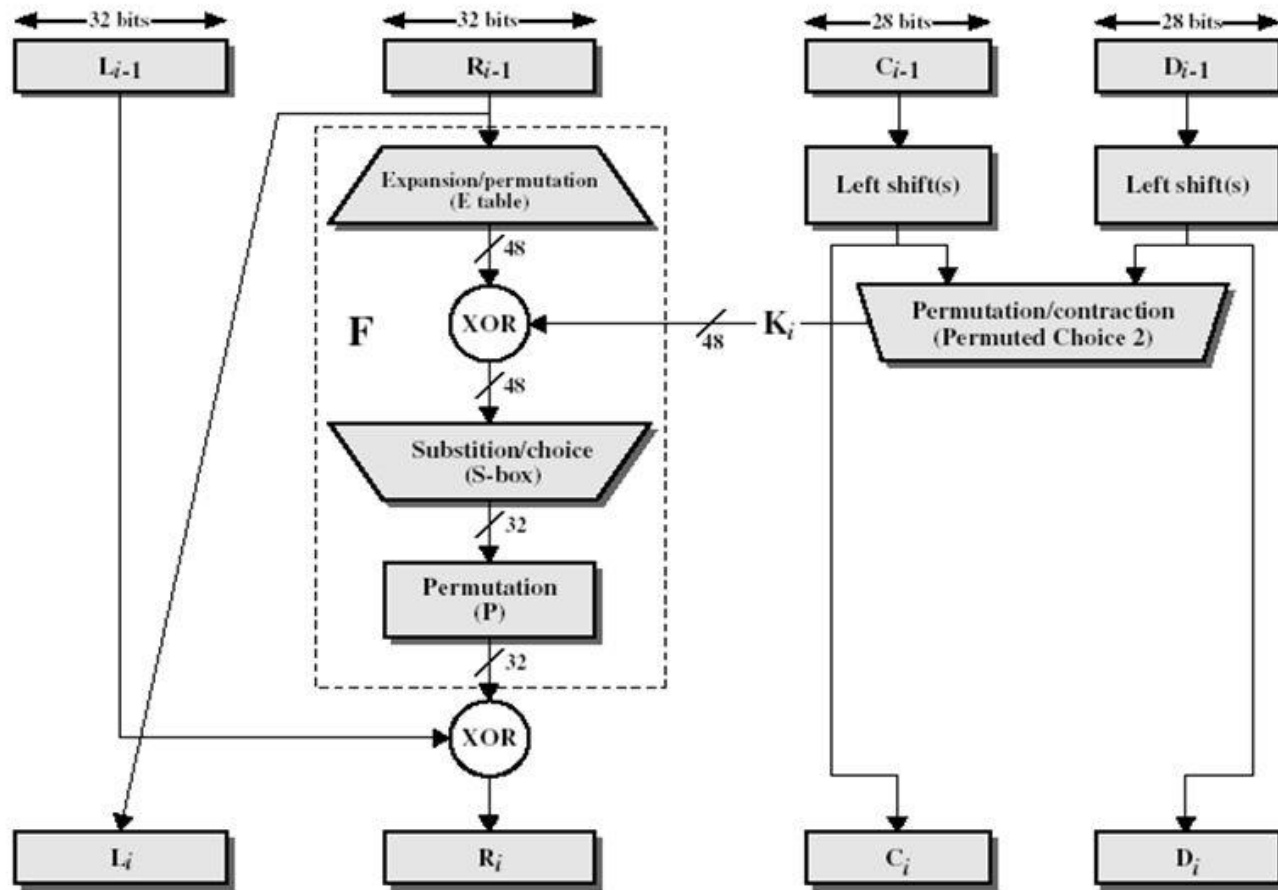
Shifting	
Rounds	Shift
1, 2, 9, 16	one bit
Others	two bits







# Single Iteration of DES Algorithm



# DES Analysis

The DES satisfies both the desired properties of block cipher. These two properties make cipher very strong.

- **Avalanche effect** – A small change in plaintext results in the very great change in the ciphertext.
  - **Completeness** – Each bit of ciphertext depends on many bits of plaintext.
- 
- Problem with DES
    - Broken in 1998 by Electronic Frontier Foundation
    - Used special purpose machine - \$250,000 <sup>a</sup>Took less than three days



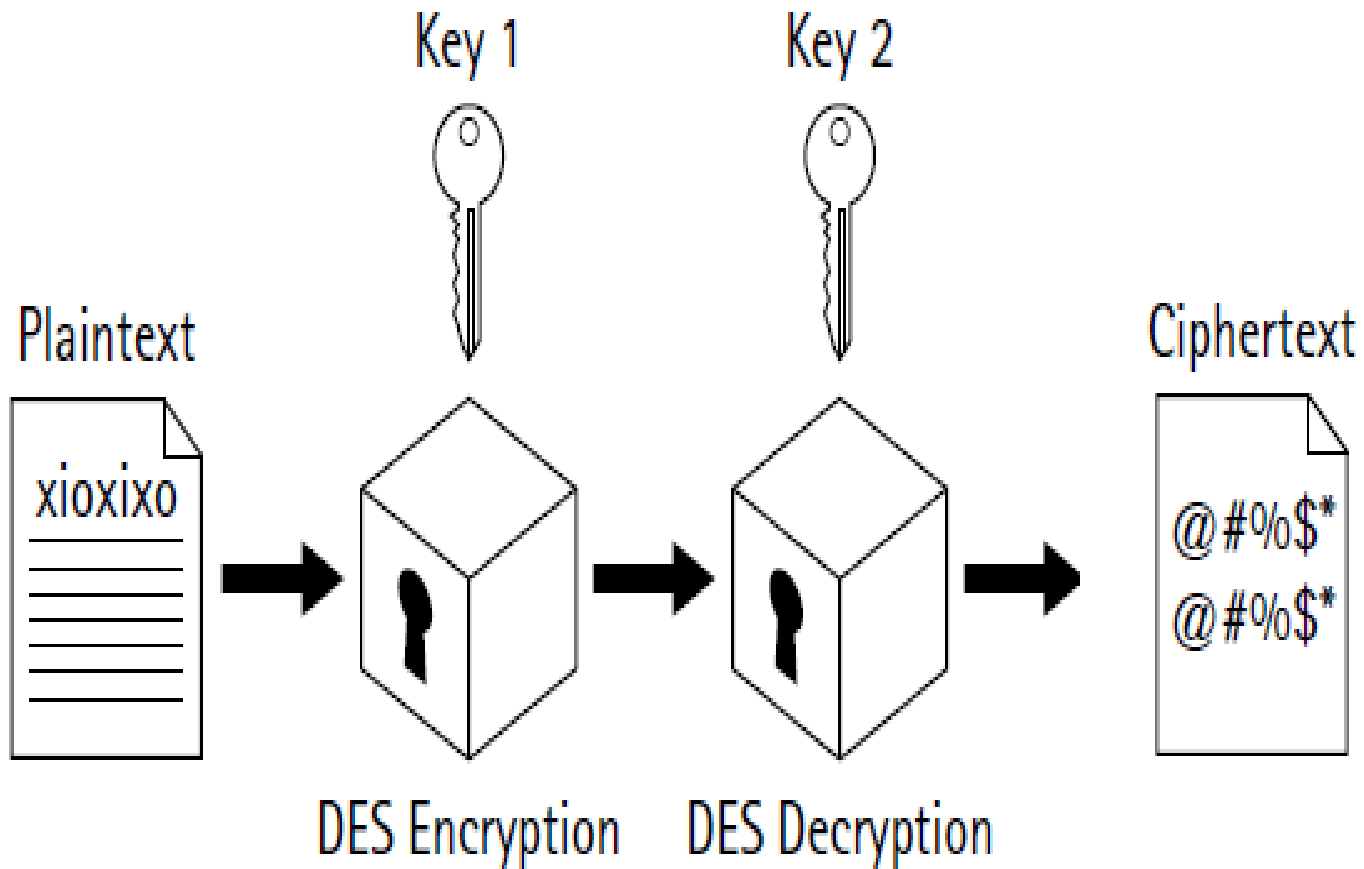
# Double DES

- DES uses a 56-bit key, this raised concerns about brute force attacks.
- Double uses two keys, K1 and K2
- Perform DES on the plaintext using K1 to get encrypt text.
- Again, perform DES on the encrypt text using K2.
- The final output is the encryption of the encrypted text.
- his leads to a  $2 \times 56 = 112$  bit key, so it is more secure than DES. Is it?
- Double DES has a 112-bit key, and ciphers blocks of 64 bits.

$$p \rightarrow E(k_1, p) \rightarrow E(k_2, E(k_1, p)) = C$$



# Double DES



# Meet-in-the-Middle Attack (MIM Attack)

- To improve the security of a block cipher, one might get the (naive) idea to simply use two independent keys to encrypt the data twice.
- In fact, an exhaustive search of all possible combinations of keys would take  $2^{2n}$  attempts (if each key  $K_1$ ,  $K_2$  is  $n$  bits long), compared to the  $2^n$  attempts required for searching a single key.
- The attacker can first compute  $E_{K_1}(P)$  for all possible keys  $K_1$  and store the results in memory (in a lookup table).
- Afterwards he can decrypt the ciphertext by computing  $D_{K_2}(C)$  for each  $K_2$ .
- Any matches between these two resulting sets are likely to reveal the correct keys. (To speed up the comparison, the  $E_{K_1}(P)$  set is stored in an in memory lookup table, then each  $D_{K_2}(C)$  can be matched against the values in the lookup table to find the candidate keys.)
- Once the matches are discovered, they can be verified with a second testset of Plaintext and Ciphertext.

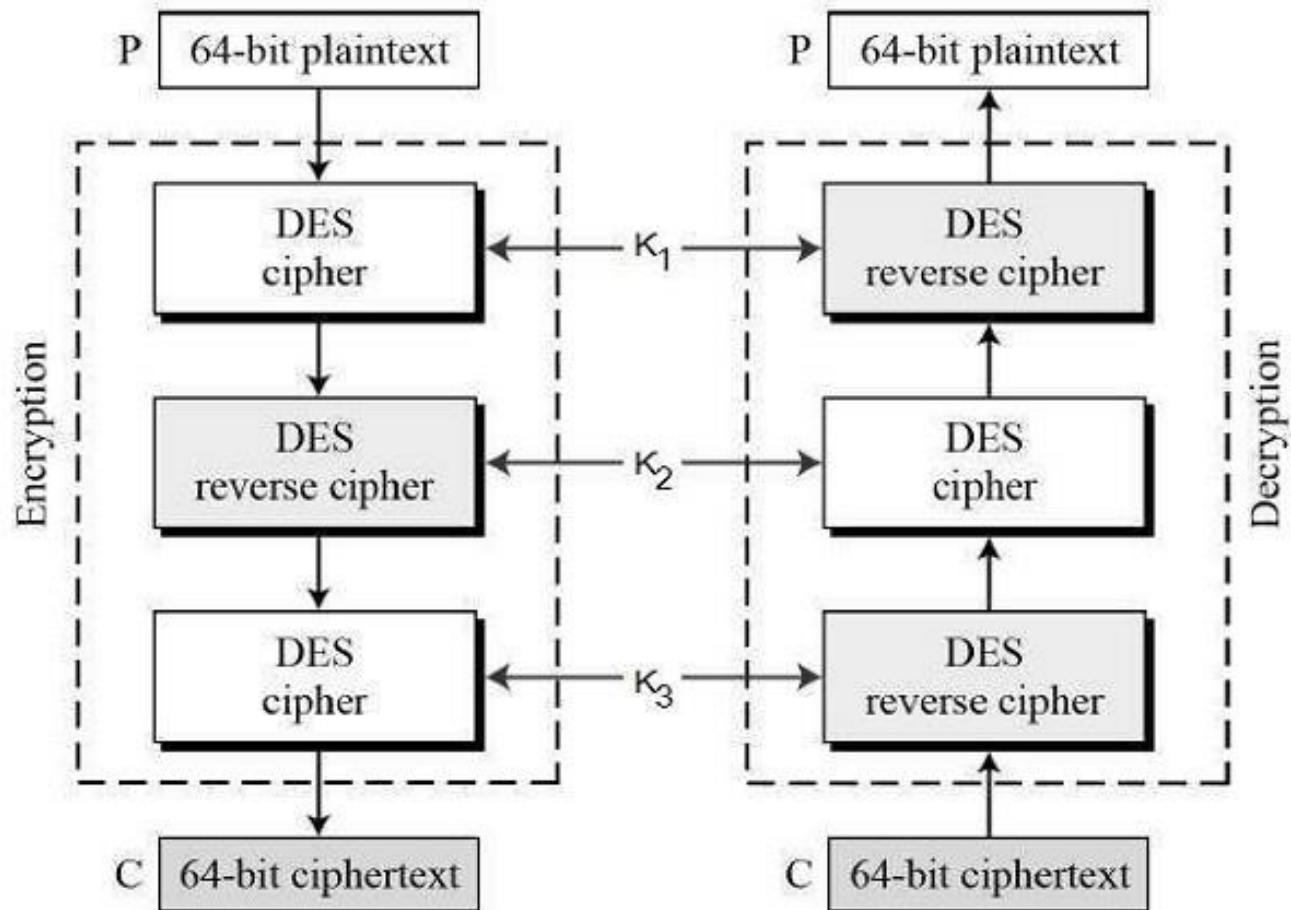


# Triple DES

- 3DES was developed in 1999 by IBM – by a team led by Walter Tuchman. 3DES prevents a meet-in-the-middle attack. 3DES has a 168-bit key and ciphers blocks of 64 bits
- The plain text block is first encrypted with  $k_1$ , then encrypted with  $k_2$  and finally with the  $k_3$
- All three keys would be different from each other
- Its three times slower than DES

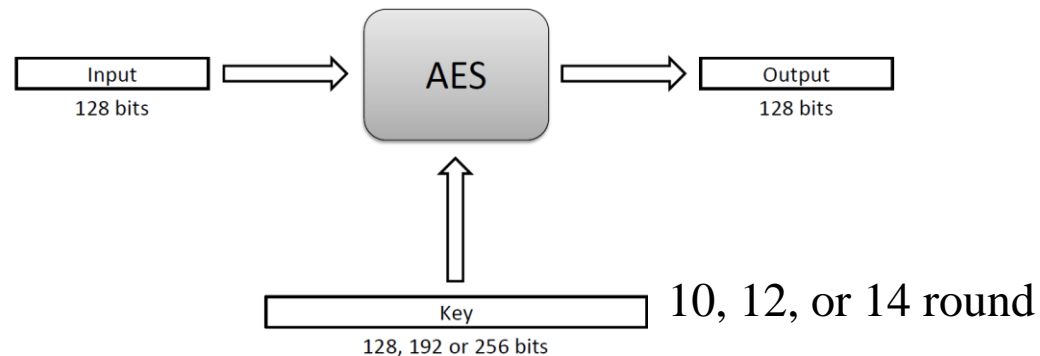


# Triple DES



# The Advanced Encryption Standard (AES)

- Clear a replacement for DES was needed
  - have theoretical attacks that can break it
  - have demonstrated exhaustive key search attacks
- can use Triple-DES – but slow, has small blocks
- US NIST issued call for ciphers in 1997
- 15 candidates accepted in June 98
- 5 were shortlisted in Aug-99
- Rijndael was selected as the AES in Oct-2000 Nov-2001



# The AES Cipher - Rijndael

- has 128/192/256 bit keys, 128 bit data
- an **iterative** rather than **Feistel** cipher
  - processes data as block of 4 columns of each 4 bytes
  - operates on entire data block in every round
- designed to have:
  - resistance against known attacks
  - speed and code compactness on many CPUs
  - design simplicity



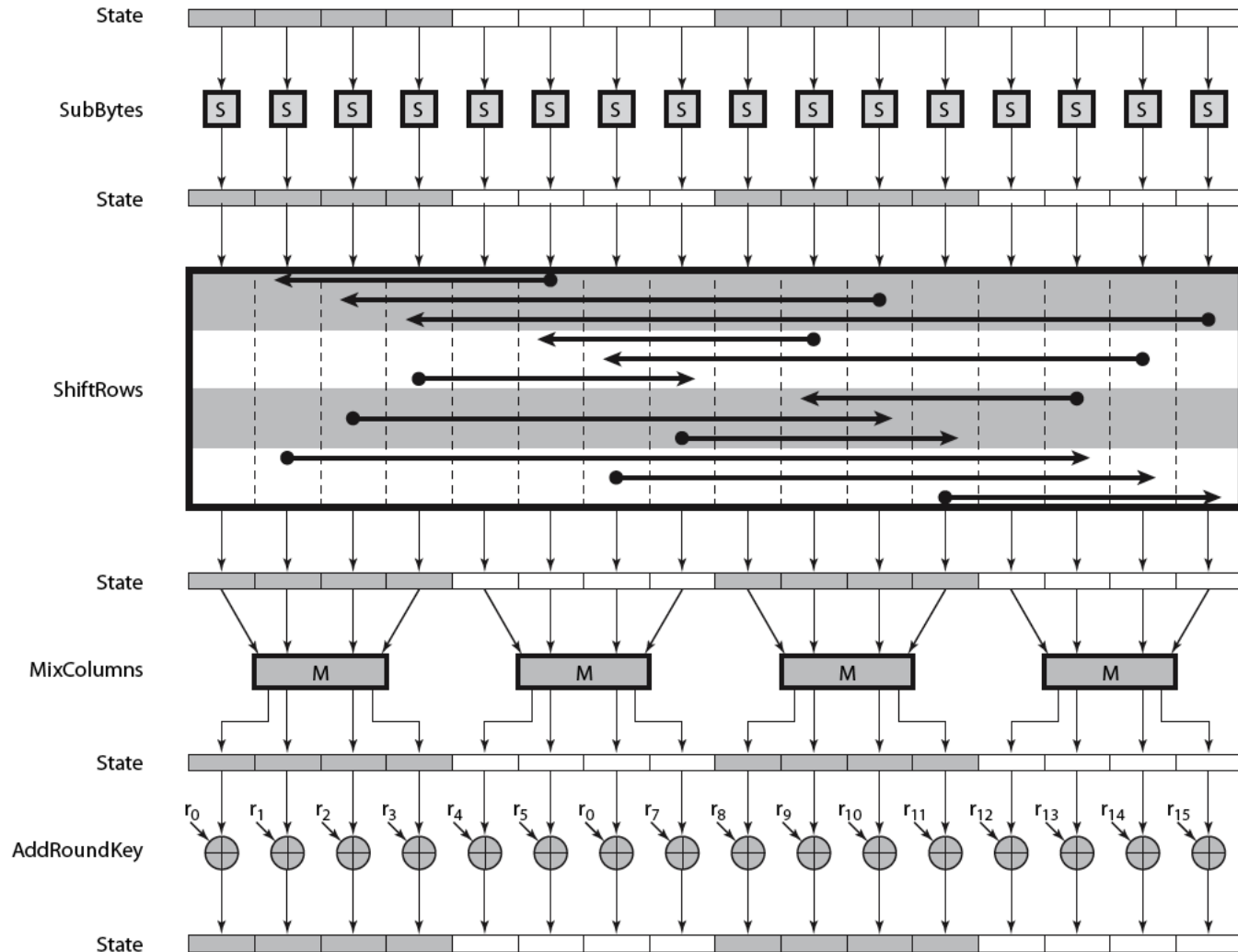
# AES Rounds

Each round is built from four basic steps:

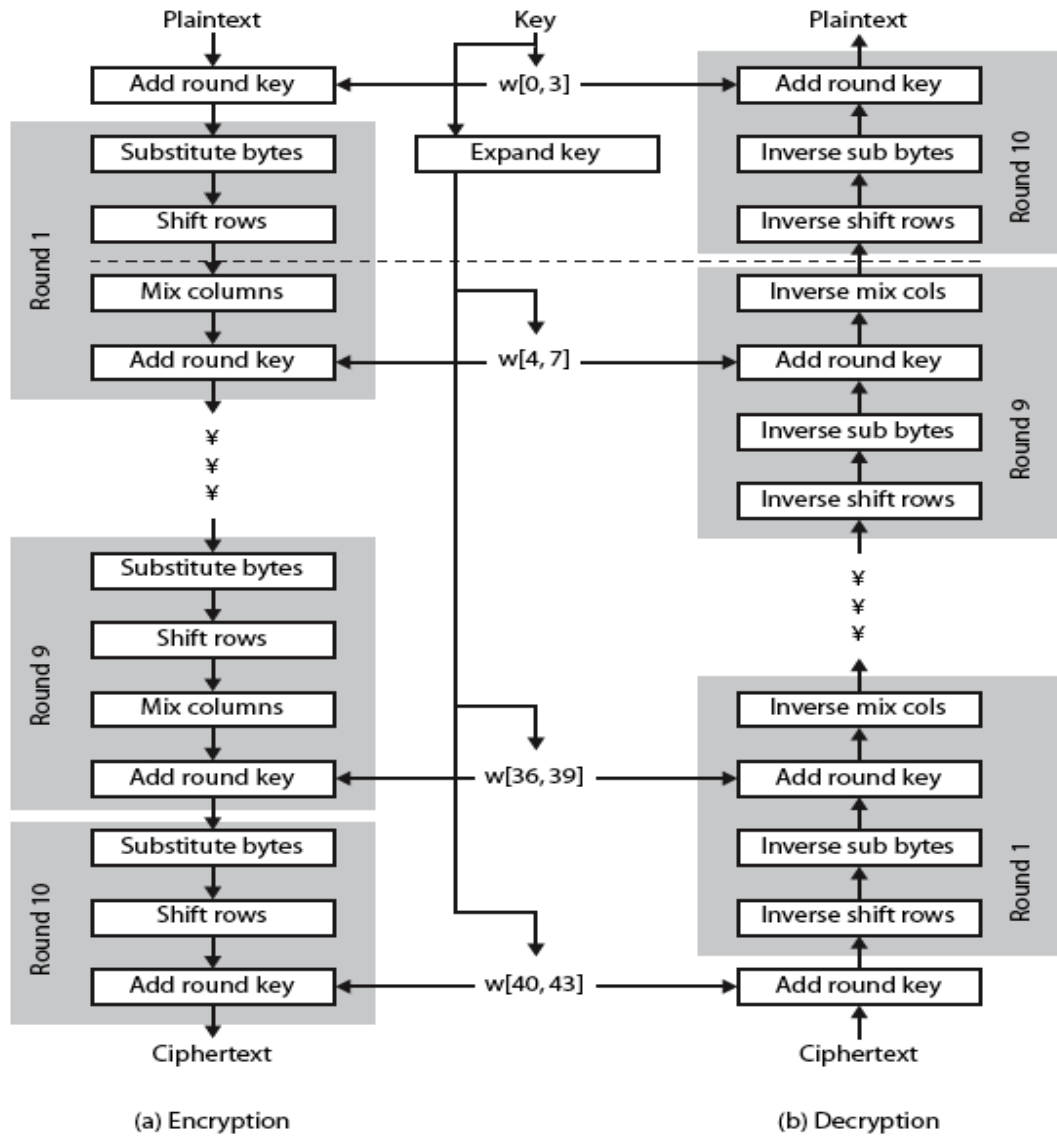
1. SubBytes step: an S-box substitution step
2. ShiftRows step: a permutation step
3. MixColumns step: a matrix multiplication step
4. AddRoundKey step: an XOR step with a round key derived from the 128/192/256-bit encryption key



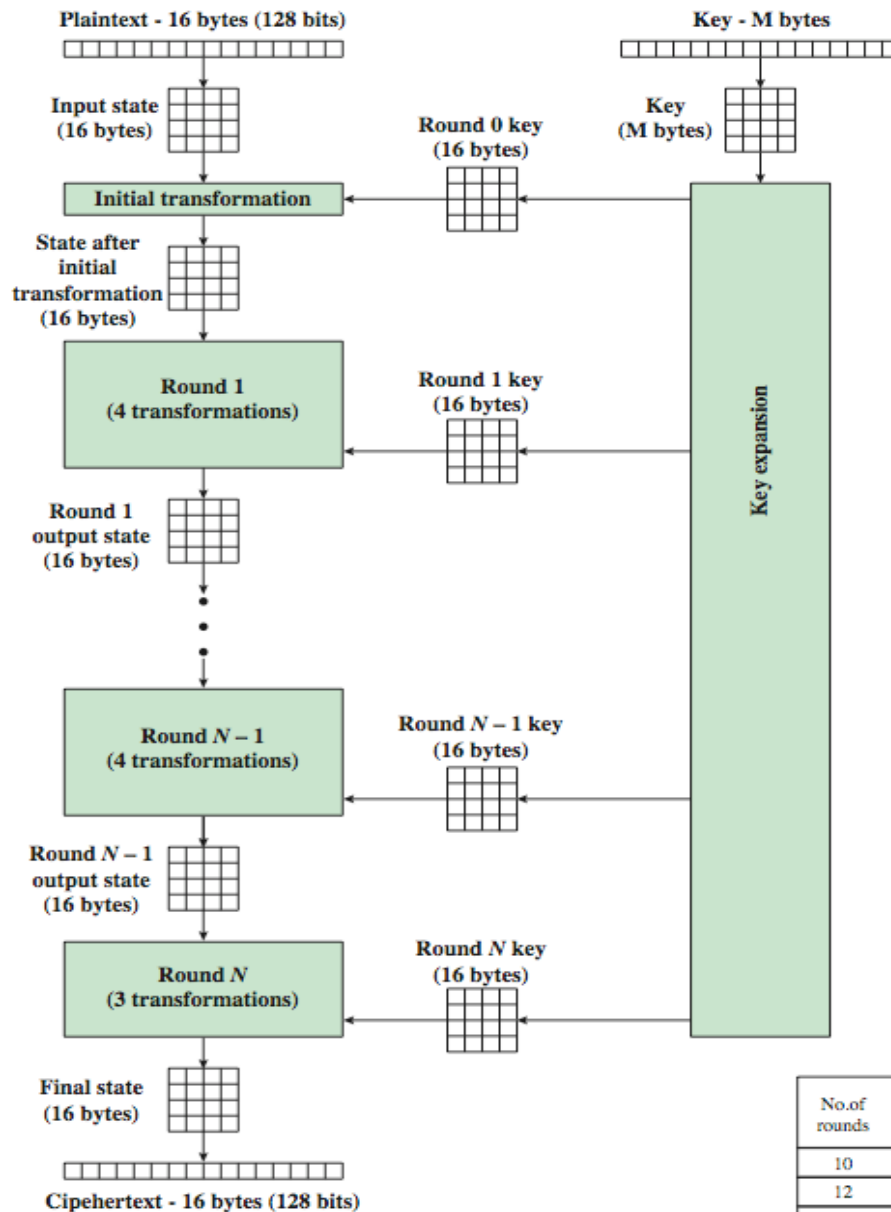
# AES Round



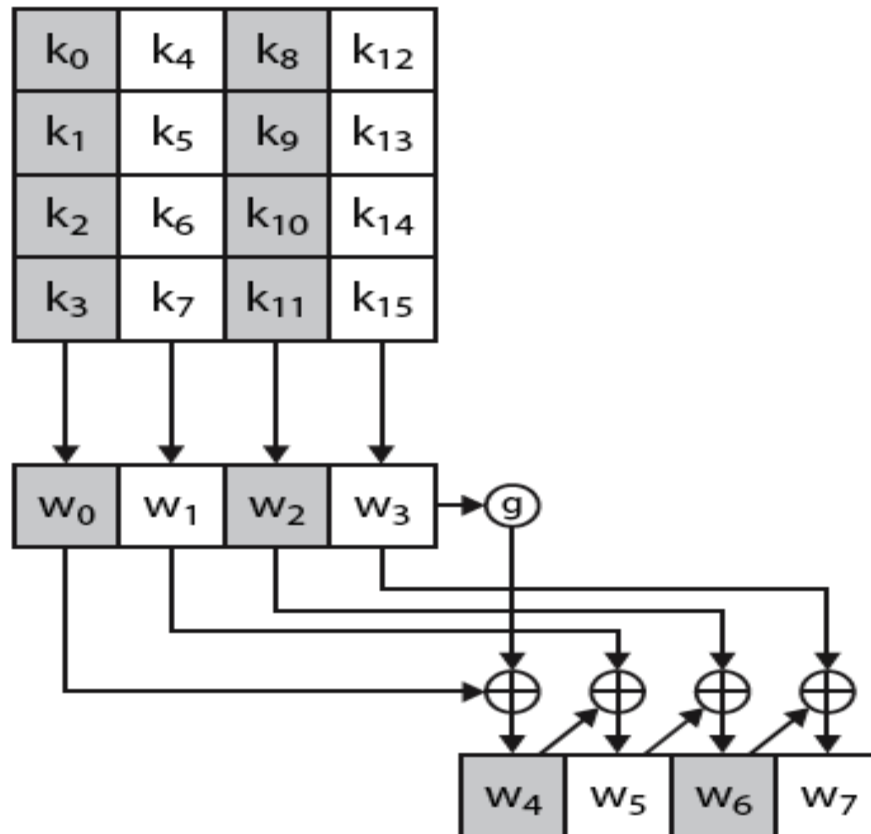
# AES Structure



# AES Encryption Process



# AES Key Expansion



# Comparison table different symmetric encryption algorithms

Symmetric Key Algorithm	Structure	Key Size (bits)	No of Rounds	Block Size (bits)	Security	Speed
DES	Feistel	56	16	64	Already Broken	Slow
3 DES	Feistel	112, 168	48	64	Adequate	Very Slow
AES	Substitution/Transposition	128, 192, 256	10, 12, 14	128	Excellent	Fast
Blowfish	Feistel	32-448	16	64	Excellent	Fast



# How to use a block cipher?

- Block ciphers encrypt fixed-size blocks
  - e.g. DES encrypts 64-bit blocks
- We need some way to encrypt a message of arbitrary length
  - e.g. a message of 1000 bytes
- NIST defines several ways to do it
  - called **modes of operation**



# Modes of Operation

- Block ciphers encrypt fixed size blocks
  - eg. DES encrypts 64-bit blocks, with 56-bit key
- Need way to use in practise, given usually have arbitrary amount of information to encrypt
  - Partition message into separate block for ciphering
- A mode of operation describes the process of encrypting each of these blocks under a single key

Some modes may use randomized addition input value



# Five Modes of Operation

- Electronic codebook mode (ECB)
- Cipher block chaining mode (CBC) – most popular
- Cipher feedback mode (CFB)



# Electronic Code Book (ECB)

The plaintext is broken into blocks,  $P_1, P_2, P_3, \dots$

Each block is encrypted independently:

$$C_i = E_K(P_i)$$

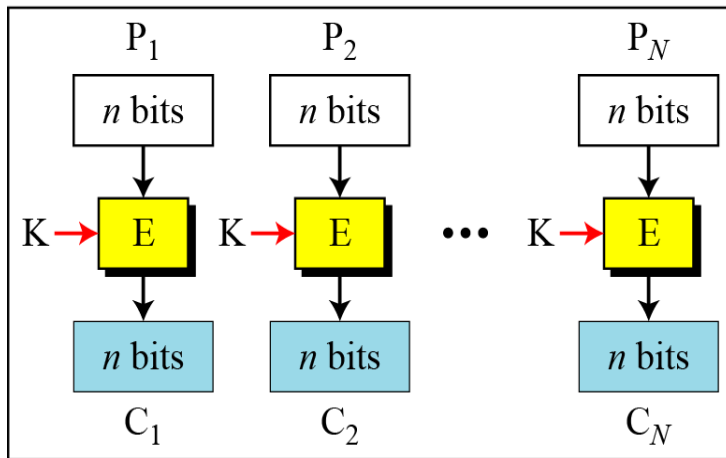
For a given key, this mode behaves like we have a gigantic codebook, in which each plaintext block has an entry, hence the name Electronic Code Book



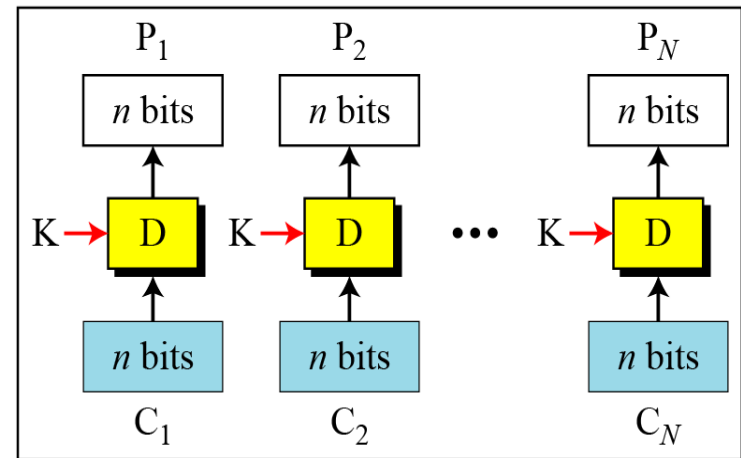
# ECB Scheme

Encryption:  $C_i = E_K(P_i)$                       Decryption:  $P_i = D_K(C_i)$

E: Encryption                      D: Decryption  
 $P_i$ : Plaintext block  $i$        $C_i$ : Ciphertext block  $i$   
K: Secret key



Encryption



Decryption



# Remarks on ECB

- Strength: it's simple.
- Weakness:
  - Repetitive information contained in the plaintext may show in the ciphertext, if aligned with blocks.
  - If the same message (e.g., an SSN) is encrypted (with the same key) and sent twice, their ciphertexts are the same.
- Typical application: secure transmission of short pieces of information (e.g. a temporary encryption key)

# Example of ECB



Original Image



Encrypted image using ECB mode



Modes other than ECB result in pseudorandomness

# Cipher Block Chaining (CBC)

- Solve security deficiencies in ECB
  - Repeated same plaintext block result different ciphertext block
- Each previous cipher blocks is chained to be input with current plaintext block, hence name
- Use Initial Vector (IV) to start process

$$C_i = E_K (P_i \text{ XOR } C_{i-1})$$

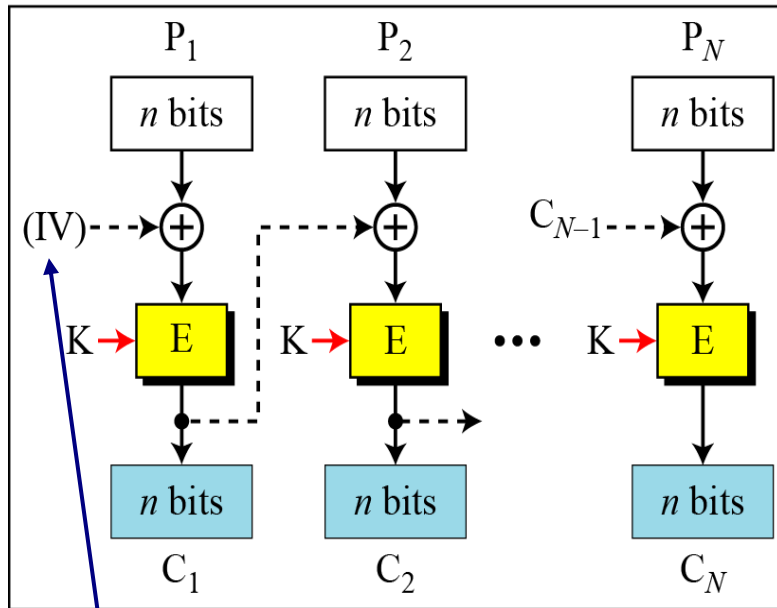
$$C_0 = IV$$

Uses: bulk data encryption, authentication

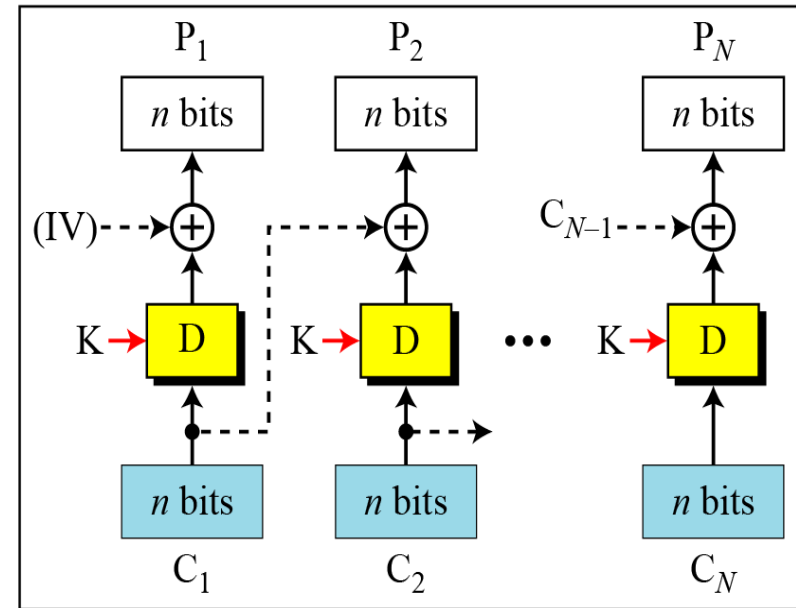


# CBC scheme

E: Encryption                    D : Decryption  
 $P_i$ : Plaintext block  $i$        $C_i$ : Ciphertext block  $i$   
 K: Secret key                    IV: Initial vector ( $C_0$ )



Encryption



Decryption

## Encryption:

$$C_0 = \text{IV}$$

$$C_i = E_K(P_i \oplus C_{i-1})$$

## Decryption:

$$C_0 = \text{IV}$$

$$P_i = D_K(C_i) \oplus C_{i-1}$$



# Cipher feedback mode (CFB) Scheme

**Encryption:**  $C_i = P_i \oplus \text{SelectLeft}_r \{E_K [\text{ShiftLeft}_r (S_{i-1}) \mid C_{i-1}]\}$

**Decryption:**  $P_i = C_i \oplus \text{SelectLeft}_r \{E_K [\text{ShiftLeft}_r (S_{i-1}) \mid C_{i-1}]\}$

E : Encryption

D : Decryption

$S_i$ : Shift register

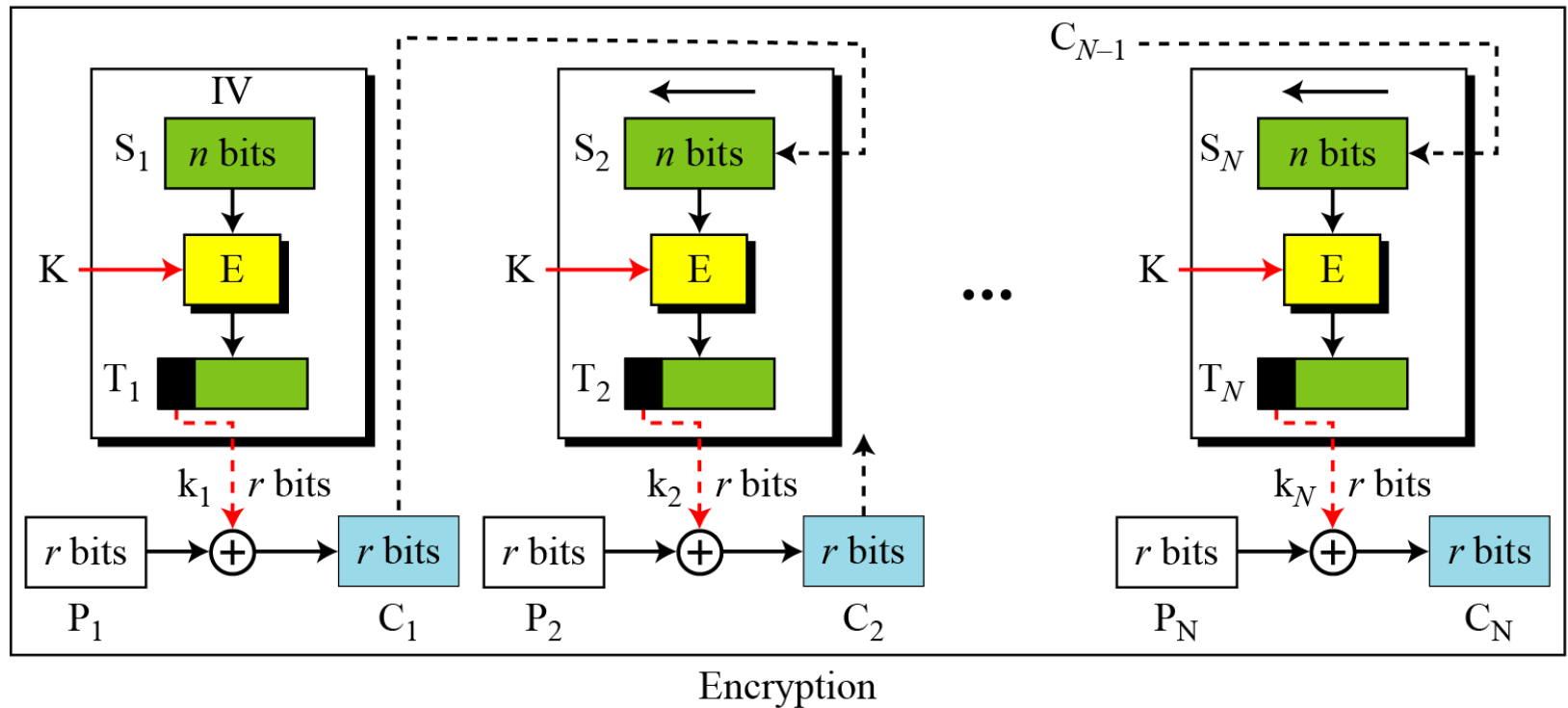
$P_i$ : Plaintext block  $i$

$C_i$ : Ciphertext block  $i$

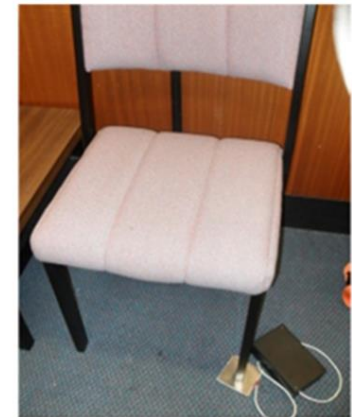
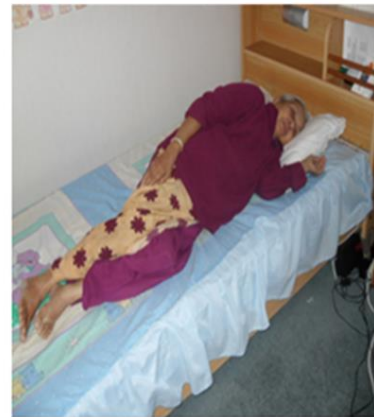
$T_i$ : Temporary register

K: Secret key

IV: Initial vector ( $S_1$ )



# Example: Designing a Secure Smart Home



# References

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